

EXPERIMENT PROCEDURE

- Measure the height of the curvature h for two watch glasses for a given distance s between the tips of the spherometer legs.
- Determine the radius of curvature R of both glasses.
- Compare the methods for both convex and concave surfaces.

OBJECTIVE

Determine the radius of curvature of various watch glasses

SUMMARY

From the height h of a spherical surface above a point on a plane defined by the corners of an equilateral triangle, the radius of curvature R of the spherical surface may be determined. This can be done for both convex and concave curvatures of the sphere.

REQUIRED APPARATUS

Quantity	Description	Item Number
1	Precision Spherometer	1002947
1	Plane Mirror	1003190
1	Set of 10 Watch Glass Dishes, 80 mm	1002868
1	Set of 10 Watch Glass Dishes, 125 mm	1002869

BASIC PRINCIPLES

A spherometer consists of a tripod with the three legs tipped by steel points and forming an equilateral triangle with sides of 50 mm. A micrometer screw, the tip of which is the point to be measured, passes through the center of the tripod. A vertical rule indicates the height h of the measured point above a plane defined by the tips of the three legs. The height of the measured point can be read off to an accuracy of $1 \mu\text{m}$ with the aid of a circular scale that rotates along with the micrometer screw.

The relationship between the distance r of all three legs from the center of the spherometer, the radius of curvature R to be determined and the height h of the surface is given by the following equation:

$$(1) \quad R^2 = r^2 + (R-h)^2$$

Rearranging for R gives:

$$(2) \quad R = \frac{r^2 + h^2}{2 \cdot h}$$

The distance r can be calculated from the length s of the sides of the equilateral triangle formed by the legs:

$$(3) \quad r = \frac{s}{\sqrt{3}}$$

Thus the relevant equation for R is as follows:

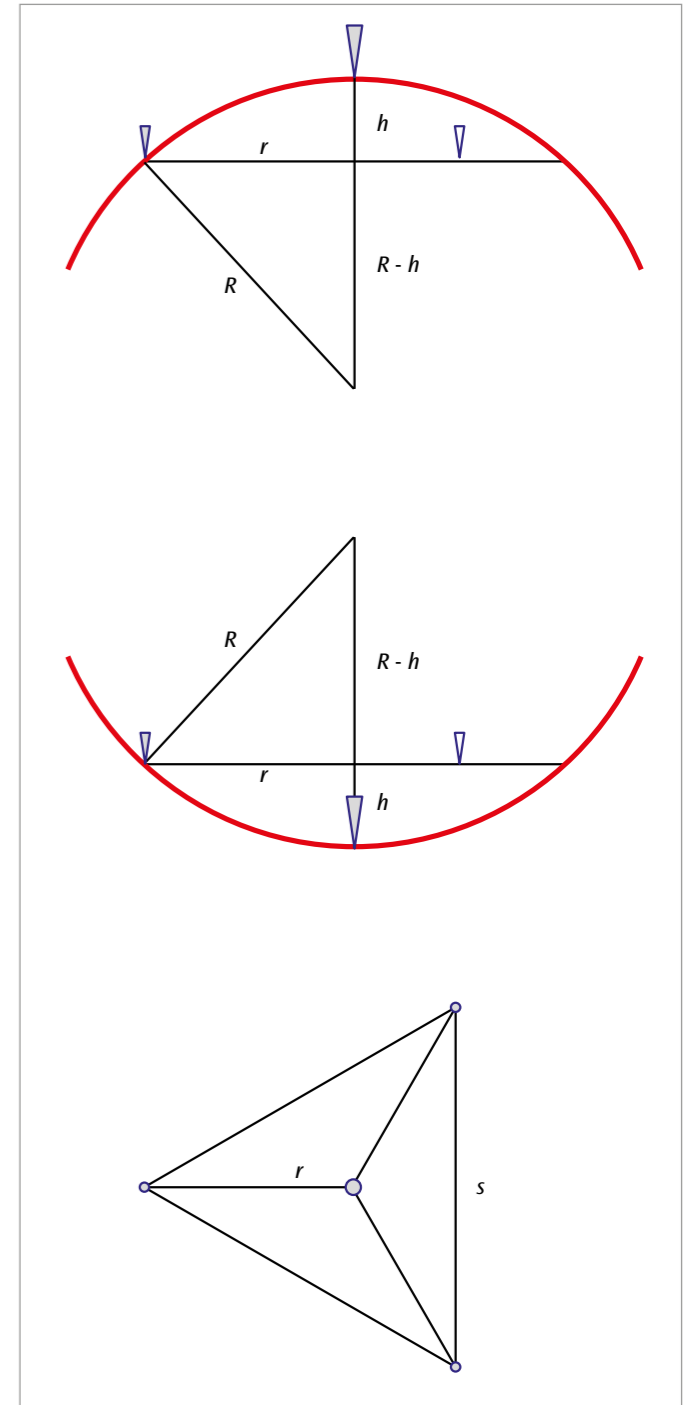
$$(4) \quad R = \frac{s^2}{6 \cdot h} + \frac{h}{2}$$

EVALUATION

The separation s between the legs of the spherometer is in this case 50 mm. When the height h is small, equation (4) can be simplified to the following:

$$R = \frac{s^2}{6 \cdot h} = \frac{2500\text{mm}^2}{6 \cdot h} \approx \frac{420\text{mm}^2}{h}$$

The scale of the spherometer allows readings for heights between 10 mm and $1 \mu\text{m}$ to an accuracy of $1 \mu\text{m}$, so that radii of curvature of about 40 mm to 400 m can be calculated.



Schematic for measurement of radius of curvature by means of a spherometer

Top: Vertical cross section for measuring an object with a convex surface

Middle: Vertical cross section for measuring an object with a concave surface

Bottom: View from above